ST. XAVIER’S COLLEGE

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**Database Management System**

**Theory Assignment #10**

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1.**Functional dependancies**

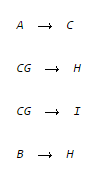
1.1 Basic concepts

Functional dependency (FD) is a set of constraints between two attributes in a relation. Functional dependency says that if two tuples have same values for attributes A1, A2,..., An, then those two tuples must have to have same values for attributes B1, B2, ..., Bn.

Functional dependency is represented by an arrow sign (→) that is, X→Y, where X functionally determines Y. The left-hand side attributes determine the values of attributes on the right-hand side[1].

**1.2 Closure of the set of functional dependencies**

1. We need to consider *all* functional dependencies that hold. Given a set *F* of functional dependencies, we can prove that certain other ones also hold. We say these ones are **logically implied** by *F*.
2. Suppose we are given a relation scheme *R*=(*A*,*B*,*C*,*G*,*H*,*I*), and the set of functional dependencies: A->B



1. Then the functional dependency tex2html_wrap_inline1194 is logically implied.

 To see why, let tex2html_wrap_inline940 and tex2html_wrap_inline946 be tuples such that

tex2html_wrap_inline1200

As we are given *A tex2html_wrap_inline1090 B*, it follows that we must also have

tex2html_wrap_inline1204

Further, since we also have *B tex2html_wrap_inline1090 H*, we must also have

tex2html_wrap_inline1208

Thus, whenever two tuples have the same value on *A*, they must also have the same value on *H*, and we can say that *A tex2html_wrap_inline1090 H*.

 The **closure** of a set *F* of functional dependencies is the set of all functional dependencies logically implied by *F*.

 We denote the closure of *F* by tex2html_wrap_inline1222 .

 To compute tex2html_wrap_inline1222 , we can use some rules of inference called **Armstrong's Axioms**:

* **Reflexivity rule:** if tex2html_wrap_inline958 is a set of attributes and tex2html_wrap_inline1158 , then tex2html_wrap_inline1058 holds.
* **Augmentation rule:** if tex2html_wrap_inline1058 holds, and tex2html_wrap_inline1234 is a set of attributes, then tex2html_wrap_inline1236 holds.
* **Transitivity rule:** if tex2html_wrap_inline1058 holds, and tex2html_wrap_inline1240 holds, then tex2html_wrap_inline1242 holds.

 These rules are **sound** because they do not generate any incorrect functional dependencies. They are also **complete** as they generate all of tex2html_wrap_inline1222 .

 To make life easier we can use some additional rules, derivable from Armstrong's Axioms:

* **Union rule:** if tex2html_wrap_inline1058 and tex2html_wrap_inline1242 , then tex2html_wrap_inline1250 holds.
* **Decomposition rule:** if tex2html_wrap_inline1250 holds, then tex2html_wrap_inline1058 and tex2html_wrap_inline1242 both hold.
* **Pseudotransitivity rule:** if tex2html_wrap_inline1058 holds, and tex2html_wrap_inline1260 holds, then tex2html_wrap_inline1262 holds.

 Applying these rules to the scheme and set *F* mentioned above, we can derive the following:

* *A tex2html_wrap_inline1090 H*, as we saw by the transitivity rule.
* *CG tex2html_wrap_inline1090 HI*by the union rule.
* *AG tex2html_wrap_inline1090 I*by several steps:
  + Note that *A tex2html_wrap_inline1090 C*holds.
  + Then *AG tex2html_wrap_inline1090 CG*, by the augmentation rule.
  + Now by transitivity, *AG tex2html_wrap_inline1090 I*.

(You might notice that this is actually pseudotransivity if done in one step.[2])

1.3 **Closure of attribute sets**

For an attriute set , + =*Closure* of under *F*

*is the set of attributes that are functionally determined by under F:* → βis in *F*+ β ⊆ +

Algorithm to compute + : *result* := ;  
 **while** (changes to *result*) **do  
 for each** β→ γ **in** *F* **do  
 begin  
 if** β⊆ *result* **then**  *result* := *result* ∪ γ   
 **end**

**EXAMPLE :**

*R = (A, B, C, G, H, I)*

*F =* {*A* → *B  
 A* → *C   
 CG* → *H  
 CG* → *I  
 B* → *H*}

(*AG)*+

*1.* result = AG

*2.* result = ABCG (A *→* C *and* A *→* B)

*3.* result = ABCGH (CG *→* H *and* CG *⊆* AGBC)

*4.* result = ABCGHI (CG *→* I *and* CG *⊆* AGBCH)

Is *AG* a candidate key?

*Is AG a super key?*

* + 1. Does *AG* → *R? ==* Is (AG)+ ⊇ R

*Is any subset of AG a superkey?*

* + 1. Does *A* → *R*? *==* Is (A)+ ⊇ R
    2. Does *G* → *R*? == Is (G)+ ⊇ R

**2**  **Decomposition**

All attributes of an original schema (*R)* must appear in the decomposition (*R*1*, R*2*):*

*R = R*1 ∪ *R*2

**2.1 Lossless-join decomposition.**  
For all possible *legal* relations *r* on schema *R*

*r =* ∏R1 (*r*) ∏R2 (*r*)

We claim the above decomposition is lossless. How can we decide whether a decomposition is lossless?

Let *R* be a relation schema.

Let *F* be a set of functional dependencies on *R*.

Let tex2html_wrap_inline1620 and tex2html_wrap_inline1622 form a decomposition of *R*.

The decomposition is a lossless-join decomposition of *R* if at least one of the following functional dependencies are in tex2html_wrap_inline1628 :

* 1. tex2html_wrap_inline1630
  2. tex2html_wrap_inline1632

Why is this true? Simply put, it ensures that the attributes involved in the natural join ( tex2html_wrap_inline1634 ) are a candidate key for at least one of the two relations.This ensures that we can never get the situation where spurious tuples are generated, as for any value on the join attributes there will be a unique tuple in **one** of the relations.

We'll now show our decomposition is lossless-join by showing a set of steps that generate the decomposition:

First we decompose *Lending-schema* into

*Branch-schema = (bname, bcity, assets)*

*Loan-info-schema = (bname, cname, loan#, amount)*

Since *bname* tex2html_wrap_inline1526 *assets bcity*, the augmentation rule for functional dependencies implies that

*bname* tex2html_wrap_inline1526 *bname assets bcity*

Since *Branch-schema* tex2html_wrap_inline1640 *Borrow-schema* = *bname*, our decomposition is lossless join.

Next we decompose *Borrow-schema* into

*Loan-schema = (bname, loan#, amount)*

*Borrow-schema = (cname, loan#)*

As *loan#* is the common attribute, and

*loan#* tex2html_wrap_inline1526 *amount bname*

This is also a lossless-join decomposition.

**2.2** **Dependencies Preservation**

1. Another desirable property in database design is **dependency preservation**.
   * We would like to check easily that updates to the database do not result in illegal relations being created.
   * It would be nice if our design allowed us to check updates without having to compute natural joins.
   * To know whether joins must be computed, we need to determine what functional dependencies may be tested by checking each relation individually.
   * Let *F* be a set of functional dependencies on schema *R*.
   * Let tex2html_wrap_inline1550 be a decomposition of *R*.
   * The **restriction** of *F* to tex2html_wrap_inline1556 is the set of all functional dependencies in tex2html_wrap_inline1628 that include only attributes of tex2html_wrap_inline1556 .
   * Functional dependencies in a restriction can be tested in one relation, as they involve attributes in one relation schema.
   * The set of restrictions tex2html_wrap_inline1660 is the set of dependencies that can be checked efficiently.
   * We need to know whether testing only the restrictions is sufficient.
   * Let tex2html_wrap_inline1662 .
   * *F*' is a set of functional dependencies on schema *R*, but in general, tex2html_wrap_inline1668 .
   * However, it may be that tex2html_wrap_inline1670 .
   * If this is so, then every functional dependency in *F* is implied by *F*', and if *F*' is satisfied, then *F* must also be satisfied.
   * A decomposition having the property that tex2html_wrap_inline1670 is a **dependency-preserving** decomposition[3].

**Reference :**

[1]” <http://www.tutorialspoint.com/dbms/database_normalization.htm>”, October 8 2015

[2]” http://www.cs.sfu.ca/CourseCentral/354/zaiane/material/notes/Chapter6/node12.html”, October 8 2015.

[3]” http://www.cs.sfu.ca/CourseCentral/354/zaiane/material/notes/Chapter7/node8.html”, October 8 2015.